ON THE E/P-COSMIC RAYS AS MEDIATORS OF VISCOUS FORCES THAT CREATE SHOCK AND VORTEX STRUCTURES IN THE RADIO GALAXIES

N.O. Tsvyk
Institute of Radio Astronomy of NAS of Ukraine, Chervonopraporna 4, 61002, Kharkiv, Ukraine, natalitsv69@gmail.com

ABSTRACT. There are for the galaxies of FRII type (like Cygnus A) studied a number of hydrodynamic and kinetic processes to transport of magnetized plasma with cosmic rays, and a stratification process of RG-lobe because of e/p-cosmic rays. We found that the jet and bow shock in radio galaxies are supported by the processes of e/p-cosmic rays (acceleration, radiation), and the effects of changes in viscosity inside the cocoon. Cosmic rays are working inside the "jet head" into the cocoon stratification: to the light cavity (with high kinematic viscosity) and to the heavy shock cover (with high magnetic viscosity). The post-jet-vortex is injected by diffusion of e-rays through the area of "jet head" MHD-turbulized, and it is flowing a caviton around. Alternatively, the bow shock accompanied super sound turbulent waves and flows with p-rays.

Keywords: Radio galaxy; cosmic rays, viscosity, shocks

1. Introduction. A history for the simulation of the FRII-type radio galaxy lobes

There was in Kaiser (1997) shown a self-consistent hydrodynamical model for the jet-cocoon of FRII radio galaxy (RG), with reconfiguration jet-shock (that connected with e-jet plasma production). The other main work, Zanni (2003), show a simple of self-consistent cocoon shock model of FRII RG; and in a work of Kino (2004) was illustrated a hot spot of two-shocks dynamic in details (the parameters of Cygnus A galaxy found).

There are Mathews (2011, 2012) recently shown a model for self-consistent evolution of gas and cosmic rays (CRs) in Cygnus A, in assuming a wind-injection of the viscous e-gas with e-CRs into the lobe (cocoon) of Radio Galaxy. This model shows the post-jet-wind with e-CRs; how e-CRs mix with cluster gas; how viscosity supports the e-wind-flow.

In work of Tsvyk (2010) was discussed a model of RG with two-layer cocoon that separated by e- and p-CRs; and this model is developed here. New points in this report: p-CRs are the shock-inductors; effects of CRs in turbulence and current production; effect of viscosity changes as flow-regulator. We grounded in main assumptions of Mathews (2012), but show the cocoon dynamics in consist with two simple physical structures: a shock-like outer-layer and a vortex-flow winding the inner-layer. The aim of this work is to study when the main structures of FRII-RG (jet, cavity-lobes and bow-shocks) are grown up because of stratification effects in the magnetized plasma through the e/p cosmic rays as mediators.

2. The main impacts of the CRs to the FRII-lobe

There key assumptions are: (1) a cocoon matter composed of electron-positron e-plasma (density of $n_e=n_{e1}+n_{e2}$), and ion-proton plasma ($n_p=n_{p0}$), atoms and neutrals ($n_n$), e- and p-CRs; (2) a cocoon matter is quasi-neutral ($n_{te}$, $n_{tp}$, $n_{tn}$) but current exists in it; (3) the CRs, that have being accelerated by DSA-mechanism near HS and bow shock, are the main mediator of exchanges due to they relativistic properties; (4) the e- and p-CRs separate in different areas because of flow dynamics and viscosity changes; (5) a magnetic field ($B$) is produced by regular part from the CR-diffusion currents, and by dynamical part (the jet elongated) from pumping in the frozen of e-flows and from the p-CR kinetic effects of mixed matters (mainly within the shock areas). Out the scope are the ions-CRs decays, e-annihilation and many other processes.

The main part of cocoon energy contains in p-CRs; and some essential part is in e-CRs too. The less part cocoon energy contains in $B$-field, but frozen effects do $B$-field rule the flow cocoon dynamics. Cocoon energy contains in the p-CRs, the e-CRs, the turbulence (waves and vortices), the thermal matter and the magnetic field. A jet consists of the e-plasma, with some part of p-plasma; but the p-flows are the most inert and energetically. The e-plasma flows are much frozen in B-fields and they fill the inner-cocoon; against to the p-plasma fills the outer cocoon and pumping shocks because of there momentum. Cocoon stratifies because of viscosity changes and injection of Hill’s vortex flows (jet-supported). The radiation of e-CRs (synchrotron in radio, IC in X-ray band) helps for e-plasma vortex glues together and separated from p-plasma turbulence flows.

The jet and the lobes parameters of RG are differ in the shock-like (Zanni, 2003) or wind-like (Mathews, 2011) models. For example, RG of Cygnus A located in cluster of $3\cdot10^{14}$ sun-mass and with Virial radius of 1Mpc. The jet length is 60 kpc, bow-shock velocity is $\sim6000$ km/s (0.02c), and the age of this source is $\sim10$ Myr (it adjusts with the observations of e-CRs radio-age, see Machalski (2007)). So, the shock-like model (Zanni, 2003) predicts the RG jet-power of $L_{j}\sim10^{47}$ erg/s and the energy of $E_{j}=3\cdot$
number of e-CRs in this area. The number of p-CRs in the outer lobe is some
part of p-plasma (~1-10%) and it is comparable to the number of e-CRs in this area.

Shock dynamic was shown in Zanni (2003). This a shock scale $R_s(t,0)$ grows with velocity $u_{sh}$ that defines from the shock presser and the ICM-plasma density, 

\[ u_{sh} = \frac{dR_s(t,0)/dt \sim (P(t)/\rho(t))^{1/2}(\cos^2 \theta + a_1), }{ } \]

and has an elongation along the jet-direction (for $\theta=0$ we have $1+a_1 \sim 1.3$). The other way, the energy of cocoon defines from the jet burst power (that comes with flow injection of e-CRs plasma), and as well as from shock presser multiplied to cocoon volume, $E_c(t) \sim I_c(t)/dt \sim P(t) R_s(t,0)^3$. The jet plasma is strongly blown to the inner lobe (3-area in fig.1), and it compresses the cluster matter of outer lobe (1-area, ICM) into the bow-shock front (2-area).

The flow velocities are super-sonic and not regular behind the shock front. Here is the turbulence dominated in plasma dynamics that pumps the Meshkov-vortex instabilities and ejects the inner-lobe-flow vortex surrounding bow-front. The e/p-CRs help to transport shock energy because there high transcalency. The jet-hot-spot, being the shock-center-point, forms the cavitation-like feature in density map (see fig.1: 3, 4-arrais) which may work to focus the wave-shock energy and support the jet.

**Vortex properties in the inner lobe-cavition area.** Some of the vortex-flow dynamic with vortex-injection was shown in Antonucci-Delogo (2010). We add this sketch of processes some more connection with shock-structures. This way, the main vortex is injected by Cariloles force in around of min-pressure-focus at jet-head (that forms a ring near the hot spots) because of flux-dynamic in the post-jet structures of e-flux-matter blows. The injection provides within Kelvin’s low frames: 

\[ \frac{d}{dt}(\rho \omega) = \frac{d}{dt}(\rho \omega) \nabla \cdot V = \text{(o-circulation is constant, } \omega = \text{rot } \bar{V}). \]

The gravity-buoyant and $P_e$-viscosity forces help us to form the vortex flux of Hill’s-2 like type

\[ R_e = \rho_e c/V_e \]

\[ [\beta=0.3, \rho_e=1-kpc] \]
in the post-jet cavity surface around (see fig.1, 3’ area), because of the matter difference and e-CR presser variation:

\[
\frac{\vec{\varepsilon} u}{\varepsilon} + \rho \frac{\partial}{\partial t} \nabla P + \vec{\nabla} \cdot (u_\perp \vec{\omega}) + \vec{F}_g + \vec{F}_e = 0.
\]

A simple model of Hill’s-2 vortex of \( R_{3,1} \) size (limited of e-plasma contact border, \( R_{3,1} \sim 0.7 \, R_* \)) may describe as main-flow-vortex in nearly uncompressed matter by the velocity profile in spherical \((r,\theta)\) geometry with the RG centre as zero-point and jet aligns to \( \theta=0 \):

\[
u_x \propto \rho_i(r)^{-1} (R_{3,1}(t, \theta) - r^2) \cos \theta \cos(2 \theta);
\]

\[
u_\theta \propto \rho_i(r)^{-1} (R_{3,1}(t, \theta) - r^2) \cos \theta \sin(2 \theta).
\]

A fine density variation is accounted as \( u \propto \rho_i(r)^{-1} \) in attached to the King’s model. This main-vortex excites the vortex-turbulence in contact with shock-surface that runs plasma density to mix by everyone small or large flow-velocity lines. The turbulence makes to shift dynamically this Hill’s vortex forward together with bow-shock surface. The plasma presser inside the macroscopic flow tube is decrease because the e-CRs are radiated, and this supports the Carioles force in Hill’s-2 vortex structure.

Vortex flux matter composed with e-plasma and e-CRs that predominates over the thermal ep-plasma in the inner cocoon part \( n_e > n_{h,th} \). This forms a cavity-vortex structure within the inner e-Lobe density field, \( \rho = n_{h,th} m_p + n_{h,m_e} \), and the Hill-2 vortex injection helps to separate the inner-matters with e-CRs from outer-matters with p-CRs. The particles are sorted by quasi-neutrality low \( (n_{e,r} - n_{e,th} = n_{h,th}) \).

The average flow velocity \( (u) \) obtains as to dominate the e-plasma flux and the relativistic e-CR diffusion flux: \( u = (\Sigma n_a m_a u_a)/\rho \) (\( a \) is types of particles: \( e_1, e_2 \) – electron/positrons, \( p \) – protons, \( a \) – neutral atoms, and \( e_3-CR \) – relativistic particles). Superposition of the vortex and the shock velocity gives up the flux relaxation \( (u \rightarrow 0) \) at \( \theta \sim \pi/2 \). Near the e-lobe edge \((R_{3,1} \text{-surface})\) we have \( u \rightarrow u_i \); and in this area the matter composition changes: the e-plasma is depressed and the thermal plasma with p-CRs is added, whist the presser is conserved.

To construct the density model (fig. 1, Table 2) we use the continuity matter equation with referred assumptions and with \( u \)-flux model chosen.

### 3. Magnetic fields impact to FRII-lobe structure

The magnetic field is grown both the dynamical and regular field parts inside the cocoon. The dynamical field is pumping from cosmic turbulence \( B_{w,th} \) field by adiabatic and alpha-pump turbulent effects; the regular part of \( B_{r} \) field induced from CR-diffusion currents.

Only estimation lobe model parameters are represented in Table 2, and the B-field calculations in this model shown in fig.2. If the current is estimated in the inner lobe because of diffusion motion of the e-CR-particles with the different singles, \( \Delta n_{e,th} \sim \Delta N_{e,CR} \sim 0.1 \, n_{h,th} \) (despite of \( n_i > n_{h,th} \) in the 3-area) and \( \Delta v = \sqrt{v_i - u} \sim \sqrt{v_{ad}} > \sim 10^6 \) cm/s (that is smaller than sound and Alfvvenic velocities, \( c_o \sim 10^7 \) cm/s), so the regular part of magnetic field give us toroidal-field of \( B_0 \sim 3 \times 10^{-5} \) G that mainly induced by radial and jet-elongate current components.

Beside this, the p-CRs diffusion give us a moves B-field lines together with cosmic matter, and pumps dynamically the turbulent field component as alpha-pump turbulent effects in (2) and HS areas (fig.1). These effects are dominated within the outer lobe that is near the bow shock-wave surface; we assume that \( B_{w,th} \propto (P_{e,CR} + P_{p,CR}) \). Stress of these turbulent fields must be \( B_{w,th} \sim 3 \times 10^{-4} \) G, compare to the regular \( B_r \)-field near the jet-HS surface.

Maximum strength of regular magnetic field \( (B_0) \) is nearly denoted to the areas of minimum plasma presser (the same as areas of with minimum of Hill’s-flow velocities). This effect comes to gluing of local e-flows with e-CRs, and it may appear as bright features (look likes as an additional HS-spot) in radio emission map of the LG-lobe. However the turbulent pumping may be so strong that to exhibit only one HS-point in the lobe map as the jet head.

**Table 2:** The model parameters of inner and outer lobe for typical FRII-RG (like Cygnus A) based on assumption of the wind-vortex-shock cocoon transformation because of the CR-flow dynamics (see the text and Table 1 in detail).

<table>
<thead>
<tr>
<th>AREA</th>
<th>3 (HS)</th>
<th>2 (HS)</th>
<th>(c-Lobe)</th>
<th>(outer)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( n_e )</td>
<td>0.001 (10^6 )</td>
<td>0.001 (10^6 )</td>
<td>0.003 (10^5 )</td>
<td>&lt;10^{-6}</td>
</tr>
<tr>
<td>( n_{h,th} )</td>
<td>0.0005 (10^6 )</td>
<td>0.0003 (10^6 )</td>
<td>&lt;10^{-5}</td>
<td>&lt;10^{-4}</td>
</tr>
<tr>
<td>( B_{r,th} )</td>
<td>0.03 (10^{-2} )</td>
<td>0.06 (10^{-2} )</td>
<td>0.03 (10^{-2} )</td>
<td>0.06 (10^{-2} )</td>
</tr>
<tr>
<td>( A_{m_e} )</td>
<td>(10^{-2} )</td>
<td>(10^{-2} )</td>
<td>(10^{-2} )</td>
<td>(10^{-2} )</td>
</tr>
<tr>
<td>( \nu_a )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
</tr>
<tr>
<td>( \nu_{e,p} )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
</tr>
<tr>
<td>( \nu_{b,c,v} )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
<td>(10^{-1} )</td>
</tr>
<tr>
<td>( R_{e,b,c,v} )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
<td>(10^1 )</td>
<td>(10^{-1} )</td>
</tr>
<tr>
<td>( \lambda_{min} )</td>
<td>(10^{-6} )</td>
<td>(10^{-6} )</td>
<td>(10^{-6} )</td>
<td>(10^{-6} )</td>
</tr>
</tbody>
</table>

\* Parameters at magnetic line intermittency \( \beta = 0.3 \); \( A \) is min CR-diff. length; \( \lambda_{min} \) is min vortex scale at \( Re=1000 \)

![Figure 2: The model of magnetic field strength (in the gray scales: dark is \( B \sim 3 \times 10^{-5} \) G, white is \( B \sim 10^{-6} \) G) and the low-band synchrotron radiation (contour lines).](image)
4. Model for the RG lobe viscosity as cosmic plasma

Cosmic plasma is low-collision matter (the collision term is $X_{\text{coll}} = \sqrt{\rho m_t} > 1$, and the magnetic presser is smaller then thermal one $P_B < P_{\text{th}}$), and this plasma is composed of the different types ($\alpha$) of particles, that parameters are changed within the RG-cocon.

The contact layer that splitting the inner lobe (3) with e-plasma and the outer lobe (2) with thermal plasma plus p-CRs, is the front of viscosity stress that comes to change the matters dynamics. Viscosity consists of kinematical and magnetic parts, and the physics of cocoon are coordi- nated by these types of viscous vary.

This way, the kinematical viscosity $\eta_k$ coordinates the changes of the velocity along $B_0$ (by $\eta_k$), and the viscous dump of transverse velocity fluctuations (by $\eta_{\text{co}}$). Here we are: $\eta_{\text{k}} \sim \eta_{\text{co}} X_0^{2-1}$, where $\eta_{\text{k}} = \frac{\Sigma (n, T, X_0)}{\eta}$ and $0<\beta<1$ is the turbulence parameter. The p- CRs make to change the characteristics $X$ and $\beta$ of the slow matter turbulence that handle the viscous forces.

The magnetic viscosity, $\eta_{\text{m}} = \rho v_{\text{m}} = \rho c^2/\sigma_{\text{eff}}$, coordinates the currents induction and the enhanced of MHD-turbulence within the shock booth and in the jet surface; both and it enhanced the magnetic dynamo in the dense matter area. Here is the effective conductivity within e-lobe depends on the neutral density $\sigma_{\text{eff}} = c^2 n_e T_e m_e^{-1} (1 + (n_e m_p)^{-1})^2 X_0^2$ as accounted in Bykov (2007) model.

Table 1 and 2 demonstrate the typical parameters in cocoon as changes of the kinematical and the magnetic viscosity, both and as turbulent exiting changes (by Reynolds number). The fig.3 demonstrates the relative viscosity changes of $v_{\text{m}}/v_0$ that response the areas where magnetic turbulence may pump strongly.

The e-CRs are radiating mainly by synchrotron (in radio bands at f-frequency) and synchrotron-inverse Compton (in X-ray bands) processes, which are frequency-dependent. So, the lobe radio brightness is $I_{\text{lo}} < n_{\text{eCR}} B f^{-\gamma~1/2}$, and the X-ray brightness depends on $n_{\text{eCR}}$ and radiation field.

The e-p-CRs flow together with the thermal plasma (that frozen in B-field tubes) and drift with energy-dependent diffusing velocity, $v_{\text{eCR}} = u + v_{\text{diff, eCR}}$. A diffusion velocity defines by turbulence parameters and regular magnetic field ($B_0$): $v_{\text{diff, eCR}} \sim (K_0/\Lambda_0)$ $\gamma^2 \times (B_0/B_{\text{max}})^2 r_p c/\Lambda_0$. Thus, the low-energy particles of e-CRs, that was cooling by radiation to energy $\gamma~1..10$, have to flow with thermal plasma better then diffuse. Alternatively, the p-CRs particles have to correct a local $B_{\text{max}}$-lines with any diffusion act, thus in a bow shock area this effects are lim- ited the magnetic field correlation scales ($\Lambda_0$) with the p-CRs energy spectrum ($\gamma_{p,\text{max}}$) and with $R(t)$ lobe-size.

This way, taking account the trends of B-field and e-flows, we may predicted that a powerful radio emission of low-energy e-CRs in MHz-band comes from areas where e-rays are pulled together into streams, due to the turbu- lence by viscous forces dumping, and e-rays cooling. And the radiation-cooling of e-CRs give us the main mediator-effects that coordinate all cocoon dynamics.

5. Radiation and streaming of the e-CRs in FRII lobe

In the inner lobe, the wind-flow consists of the local flows with e-CRs which are gluing because of viscosity, magnetize effects and radiating cooling of e-CRs. The diffusion effect of the e-CRs, because of vortex and Al- fven-wave turbulence, are smoothing the flow dynamic and dumping turbulence by viscosity driven. The effect of e-CRs radiation leads to cool of the lobe matter and it helps a current production and gluing of local e-CR-flows.

Figure 3: The model of relative viscosity changes (in the gray scales: dark is $v_{\text{m}}/v_0 \sim 10^{-10}$, white is $v_{\text{m}}/v_0 \sim 10^{-20}$; the 2-3 contact $R_d$-boundary outline schematically sketched).

6. Conclusions

1. The viscosity of RG matter rules in the lobe-phenomenology. It is switching the instabilities, and dir- ecting the gluing flows, and heating or accelerating of CRs in the cocoon, and the magnetic-viscosity divides the vortexes into small modes ($B$-pumping).

2. The bow-shock transports by wave-turbulence, and by the p-CRs, that getting up of magnetic-viscosity the biggest. The e-p-CRs ects by diffusion-shock acceleration mechanism.

3. The magnetic field turbulence prevents the mixing of cocoon fluid. The e-CRs frozen into magnetic turbulence critically, beginning with $>10^2$ pc-size modes (the smallest). The p-CRs help to mix the matters.

4. The e-CRs and p-CRs are separated by injection of Hill’s-2 vortex from relativistic post-jet e-plasma-flow winding. The ties of e-CRs are gluing by viscosity and radiate-cooling effects.

5. The e-CRs diffuse (in adding to flow-transport) by energy-dependent, because of B-turbulence that has been generated by vortexes and MHD-waves.

After synchrotron-radiate-cooling, the low-energy e-CRs are filling nearly all cocoon-volume, adding to the p-CRs that holding up the B-turbulence within the cocoon-surface.

References