SOFT GAMMA REPEATERS AND ANOMALOUS X-RAY PULSARS BEYOND MAGNETARS

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ABSTRACT. The observational properties of Soft Gamma Repeaters and Anomalous X-ray Pulsars (SGR/AXP) indicate to necessity of the energy source different from a rotational energy of a neutron star. The model, where the source of the energy is connected with a magnetic field dissipation in a highly magnetized neutron star (magnetar) is analyzed. Some observational inconsistencies are indicated for this interpretation. Slow rotating radiopulsars with very high magnetic fields were discovered, which don’t show any features of SGR, there are SGR/AXP in which an upper limit of the dipole magnetic field strength corresponds to average magnetic field of radio pulsars. The energy source, connected with the nuclear energy of superheavy nuclei stored in the nonequilibrium layer of low mass neutron star is discussed. The losses of rotational energy, observed in SGR/AXP are connected with a magnetised stellar wind, induced by the bursting events near the neutron star surface.

Keywords: Stars: neutron - stars: magnetars - stars: activity

1. Introduction

Neutron stars (NS) are formed as a result of a collapse of the core of a massive star with a mass $M > \sim 12M_\odot$. Conservation of the magnetic flux gives an estimation of NS magnetic field as $B_{ns} = B_s(R_s/R_{ns})^2$, $B_s = 10 \div 100$ Gs, at $R \sim (3 \div 10)R_\odot$, $R_{ns} = 10$ km, $B_{ns} = 4 \cdot 10^{11} \div 5 \cdot 10^{13}$ Gs (Ginzburg, 1964).

Estimation of the NS magnetic field is obtained in radio pulsars by measurements of their rotational period and its time derivative, in the model of a dipole radiation, or pulsar wind model (Pacini, 1967; Goldreich & Julian, 1969) Timing observations of single radiopulsars give the following estimation $B_{ns} = 2 \cdot 10^{11} \div 5 \cdot 10^{13}$ Gs (Lorimer, 2005).

Figure 1: $P - \dot{P}$ diagram for radiopulsars. Pulsars in binary systems with low-eccentricity orbits are encircled, and in high-eccentricity orbits are marked with ellipses. Stars show pulsars suspected to be connected with supernova remnants, from Lorimer (2005).

The pulsars with a small magnetic field in the left lower angle decrease their magnetic field during recycling by accretion in a close binary. See Bisnovatyi-Kogan (2006).

SGR are single neutron stars with periods 2 $\div$ 8 seconds. They produce “giant bursts”, when their luminosity $L$ in the peak increase $5 \div 6$ orders of magnitude. Having a slow rotation, and small rotational energy, their observed average luminosity exceeds rotational loss of energy more than 10 times, and orders of magnitude during the giant outbursts.

It was suggested by Duncan and Thompson (1995), that the source of energy is their huge magnetic field, 2 or 3 order of a magnitude larger, then the average field in radiopulsars. Such objects were called magnetars.
2. SGR, giant bursts, and short GRB

First two Soft Gamma Repeaters (SGR) had been discovered by KONUS group in 1979. The first one, FXP 0520 - 66, was discovered after the famous giant 5 March 1979 burst (Mazets et al., 1979b,c; Golenetskii et al., 1979), see also Mazets et al. (1982). In another source B1900+14 only small recurrent bursts had been observed (Mazets et al., 1979a). Now these sources are known under names SGR 0520 - 66 and SGR 1900+14 respectively. The third SGR 1806-20 was identified as a repetitive source by Laros et al. (1986a,b). The first detection of this source as GRB070179 was reported by Mazets et al.(1981), and it was indicated by Mazets et al. (1982), that this source, having an unusually soft spectrum, can belong to a separate class of repetitive GRB, similar to FXP0520 - 66 and B1900+14. This suggestion was completely confirmed. The forth known SGR1627-41, showing giant burst, was discovered in 1998 almost simultaneously by BATSE (Kouveliotou et al., 1998a), and BeppoSAX (Feroci et al., 1998). The giant bursts had been observed until now in 4 sources.

2.1. SGR0526-66

It was discovered due to a giant burst of 5 March 1979, projected to the edge of the SNR N49 in LMC, and described by (Mazets et al. 1979b,c; Golenetskii et al. 1979, Mazets et al. 1982). Accepting the distance 55 kpc to LMC, the peak luminosity in the previous case, it leads to the pulsar age \( \tau_p = 5 \times 10^{-11} \) years, much smaller that the age of SNR, estimated by 10^4 years. These values of \( P \) and \( \dot{P} \) correspond to the rate of a loss of rotational energy \( \dot{E}_{\text{rot}} = 3.5 \times 10^{34} \text{ ergs/s} \), and magnetic field \( B = 8 \times 10^{14} \text{ G} \). The age of the pulsar estimated as \( \tau_p = P/2\dot{P} = 700 \) years is much less than the estimated age of the close nearby SNR. Note that the observed X-ray luminosity of this object \( L_x = 2 \times 10^{35} - 2 \times 10^{36} \text{ ergs/s} \) is much higher, than rate of a loss of rotational energy, what means that rotation cannot be a source of energy in these objects. It was suggested that the main source of energy comes from a magnetic field annihilation, and such objects had been called as magnetars by Duncan and Thompson (1992).

2.2. SGR1900+14

Recurrent bursts from this source had been first observed by Mazets et al. (1979a). Detailed observations of this source are described by Mazets et al. (1999b,c), Kouveliotou et al. (1999), Woods et al. (1999). The giant burst was observed 27 August, 1998. The source lies close to the less than 10^7 year old SNR G42.8+0.6, situated at distance \( \sim 10 \) kpc. Pulsations had been observed in the giant burst, as well as in the X-ray emission observed in this source in quiescence by RXTE and ASCA. \( \dot{P} \) was measured, being strongly variable. Accepting the distance 10 kpc, this source had in the region \( E_\gamma > 15 \) keV: \( L_p > 3.7 \times 10^{44} \text{ ergs/s} \), \( Q_p > 6.8 \times 10^{43} \text{ ergs} \), \( Q_t = 5.2 \times 10^{43} \text{ ergs} \), \( L_{\gamma}^{\text{rec}} = 2 \times 10^{40} - 4 \times 10^{41} \text{ ergs/s} \), \( Q_{\gamma}^{\text{rec}} = 2 \times 10^{39} - 6 \times 10^{41} \text{ ergs} \), \( P = 5.16 \text{ s} \). The X-ray pulsar in the error box of this source was discovered by Hurley et al. (1999b). This source was discovered also in radio band, at frequency 111 MHz as a faint, \( L_{\text{radio max}} = 50 \text{ mJy} \), radiopulsar (Shitov, 1999), with the same \( P \) and variable \( \dot{P} \), good corresponding to X-ray and gamma-ray observations. The values of \( P \) and average \( \dot{P} \) correspond to the rate of a loss of rotational energy \( \dot{E}_{\text{rot}} = 3.5 \times 10^{34} \text{ ergs/s} \), and magnetic field \( B = 8 \times 10^{14} \text{ G} \). The age of the pulsar estimated as \( \tau_p = P/2\dot{P} = 700 \) years is much less than the estimated age of the close nearby SNR. Note that the observed X-ray luminosity of this object \( L_x = 2 \times 10^{35} - 2 \times 10^{36} \text{ ergs/s} \) is much higher, than rate of a loss of rotational energy, what means that rotation cannot be a source of energy in these objects. It was suggested that the main source of energy comes from a magnetic field annihilation, and such objects had been called as magnetars by Duncan and Thompson (1992).

2.3. SGR1806-20

The giant burst from this source was observed in December 27, 2004 (Palmer et al., 2005; Mazets et al., 2005; Frederiks et al., 2007a). Recurrent bursts had been studied by Kouveliotou et al. (1998b), Hurley et al. (1999a). Connection with the Galactic radio SNR G10.0-03 was found. The source has a small but significant displacement from that of the non-thermal core of this SNR. The distance to SNR is estimated as 14.5 kpc. The X-ray source observed by ASCA and RXTE in this object shows regular pulsations with a period \( P = 7.47 \) s, and average \( \dot{P} \) is \( 8.3 \times 10^{-11} \) s/s. As in the previous case, it leads to the pulsar age \( \tau_p \sim 1500 \) years, much smaller that the age of SNR, estimated by 10^4 years. These values of \( P \) and \( \dot{P} \) correspond to \( B = 8 \times 10^{14} \text{ Gs} \). \( \dot{P} \) is not constant, uniform set of observations by RXTE gave much smaller and less definite value \( \dot{P} = 2.8(1.4) \times 10^{-11} \) s/s, the value in brackets gives 1\( \sigma \) error. The peak luminosity in the burst reaches \( L_x^{\text{rec}} \sim 10^{41} \text{ ergs/s} \) in the region 25-60 keV, the X-ray luminosity in 2-10 keV band is \( L_x \approx 2 \times 10^{35} \text{ ergs/s} \) is also much higher than the rate of the loss of rotational energy (for average \( \dot{P} \)). It was detected by many satellites: Swift, RXS, Konus-Wind, Coronas-F, Integral, HEND et al.

Very strong luminosity of this outburst permitted to observe the signal, reflected from the moon by the HELICON instrument on the board of the satellite...
Coronas-F, what permitted to reconstruct a full light curve of the outburst (Mazets et al., 2005; Frederiks et al., 2007a).

2.4. SRG1627-41

Here the giant burst was observed 18 June 1998, in addition to numerous soft recurrent bursts. Its position coincides with the SNR G337.0-0.1, assuming 5.8 kpc distance. Some evidences was obtained for a possible periodicity of 6.7 s, but giant burst did not show any periodic signal (Mazets et al., 1999a), contrary to three other giant burst in SGR. The following characteristics had been observed with a time resolution 2 ms at photon energy $E_\gamma > 15$ keV: $L_p \sim 8 \times 10^{43}$ ergs/s, $Q_p \sim 3 \times 10^{42}$ ergs. No tail of the giant burst had been observed. $L_{rec}^p = 4 \times 10^{40} - 4 \times 10^{41}$ ergs/s, $Q_{rec} = 10^{39} - 3 \times 10^{40}$ ergs. Periodicity in this source is not certain.

2.5. SRG giant bursts in other galaxies

The similarity between giant bursts in SGR, and short GRB was noticed by by Mazets et al. (1999c), Bisnovatyi-Kogan (1999). The experiment KONUS-WIND had observed two short GRB, interpreted as giant bursts of SGR. The first one, GRB070201, was observed in M31 (Andromeda), 1 February, 2007. The energy of the burst is equal to $1 \cdot E^{45}$ erg, in consistence with giant bursts of other SGR Mazets et al. (2008). The second short burst, GRB051103, was observed in the galaxy M81, 3 November 2005. The energy of the burst is equal to $7 \cdot E^{46}$ erg (Golenetskii et al., 2005; Frederiks et al., 2007).

3. Estimations of the magnetic fields in SGR/AXP

Despite the fact, that rotation energy losses are much smaller than the observed luminosity, for estimation of the magnetic field strength in these objects used the same procedure as in radio pulsars, based on measurements of $P$ and $\dot{P}$. The first measurements have been done for SGR 1900 + 14, in different epochs by measurements of satellites RXTE and ASCA (Kouveliotou et al., 1999), presented in Figs.2-4.

The pulse shape is changing from one epoch to another, inducing errors in finding derivative of the period. The big jump in $P$, visible in Fig 4 looks out surprising, for magnetic dipole losses, because it needs a considerable jump in the magnetic field strength, prohibited by self induction effects. Contrary, in the model of pulsar wind rotational energy losses it looks quite reasonable, that these losses strongly increase during the giant burst, when the $\dot{P}$ jump was observed.

4. Radiopulsars with very high magnetic fields and slow rotation

Radio pulsars are rotating neutron stars that emit beams of radio waves from regions above their magnetic poles. Popular theories of the emission mechanism require continuous electron-positron pair production, with the potential responsible for accelerating the particles being inversely related to the spin period. Pair production will stop when the potential drops below a threshold, so the models predict that radio emission will cease when the period exceeds a value that depends on the magnetic field strength and configuration. It was shown by Young et al. (1999a,b) that the pulsar J2144-3933 has a period of 8.51s, which is by far the longest of any known radio pulsar. Moreover, under the usual model assumptions, based on the neutron-star

Figure 2: The epoch folded pulse profile of SGR 1900 + 14 (2-20 keV) for the May 1998 RXTE observations, from Kouveliotou et al. (1999).

Figure 3: The epoch folded pulse profile of SGR 1900 + 14 (2-20 keV) for the August 28, 1998 RXTE observation. The plot is exhibiting two phase cycles, from Kouveliotou et al. (1999).
equations of state, this slowly rotating pulsar should not be emitting a radio beam. Therefore either the model assumptions are wrong, or current theories of radio emission must be revised. The period 8.51 second is characteristic for SGR/AXP objects, but this pulsar does not show any violent behaviour, and behave like ordinary radio pulsar.

Soon after this discovery, several other radio pulsars were found, where also \( \dot{P} \), and therefore magnetic field strength was measured (Manchester et al., 2001; Camilo et al., 2000; McLaughlin et al., 2003; 2004). These pulsars include:

1. PSR J1119 - 6127, \( P = 0.407 \) s,
   \[ \dot{P} = 4.0 \cdot 10^{-12} \text{ s/s}, B = 4.1 \cdot 10^{13} \text{ G}; \]
2. PSR J1814 - 1744, \( P = 3.975 \) s,
   \[ \dot{P} = 7.4 \cdot 10^{-13} \text{ s/s}, B = 5.5 \cdot 10^{13} \text{ G}; \]

It was noted by Camilo et al. (2000), that "Both PSR J1119 6127 and PSR J1814 1744 show apparently normal radio emission in a regime of magnetic field strength where some models predict that no emission should occur. Also, PSR J1814 1744 has spin parameters similar to the anomalous X-ray pulsar (AXP) IE 2259 + 586, but shows no discernible X-ray emission. If AXPs are isolated, high magnetic field neutron stars (magnetars), these results suggest that their unusual attributes are unlikely to be merely a consequence of their very high inferred magnetic fields."

3. PSR J1847 - 0130, \( P = 6.7 \) s,
   \[ \dot{P} = 1.3 \cdot 10^{-12} \text{ s/s}, B=9.4 \cdot 10^{13} \text{ G}. \]

It was noted in the paper of McLaughlin et al. (2003), with the title "PSR J18470130: A RADIO PULSAR WITH MAGNETAR SPIN CHARACTERISTICS", that "The properties of this pulsar prove that inferred dipolar magnetic field strength and period cannot alone be responsible for the unusual high-energy properties of the magnetars and create new challenges for understanding the possible relationship between these two manifestations of young neutron stars."

4. PSR J1718 - 37184, \( P = 3.4 \) s,
   \[ B = 7.4 \cdot 10^{13} \text{ G}. \]

It was noted in the paper of McLaughlin et al. (2004), that "These fields are similar to those of the anomalous X-ray pulsars (AXPs), which growing evidence suggests are magnetars. The lack of AXP-like X-ray emission from these radio pulsars (and the non-detection of radio emission from the AXPs) creates new challenges for understanding pulsar emission physics and the relationship between these classes of apparently young neutron stars."

5. SGR/AXP with low magnetic fields and moderate rotation

SGR/AXP J1550-5418 (1E 1547.0-5408) was visible in radio band, showing pulsations with a period \( P = 2.069 \) s (Camilo et al., 2007). The pulsations with the same period have been observed first only in the soft X ray band by XMM-Newton (Halpern et al., 2008). In the hard X-ray region statistics of photons was not enough for detection of pulsations. In the strong outbursts in 2008 October and in 2009 January and March, observed by Fermi gamma-ray burst monitor, the period of 2.1s was clearly visible up to the energy \( \sim 110 \text{ keV} \) (Kaneko et al., 2010). The INTEGRAL detected pulsed soft gamma-rays from SGR/AXP 1E1547.0-5408 during its Jan-2009 outburst, in the energy band 20 ÷ 150 keV, showing a periodicity with \( P=2.1 \)s (Kuiper et al., 2009). This object is the only SGR/AXP with a relatively low period, all previous has periods exceeding \( 4s \).

A low-magnetic-field SGR0418+5729 was detected by Fermi gamma-ray burst detector (Rea et al., 2010). This soft gamma repeater with low magnetic field SGR0418+5729 was recently detected after it emitted bursts similar to those of magnetars. It was noted by Rea et al. (2010) that "X-ray observations show that its dipolar magnetic field cannot be greater than 7.5 \cdot 10^{12} \text{ Gauss}, well in the range of ordinary radio pulsars, implying that a high surface dipolar magnetic field is not necessarily required for magnetar-like activity."

6. The Magnetar Model

In the paper of Duncan and Thompson (1992) was claimed, that dynamo mechanism in the new born rapidly rotating star may generate NS with a very strong magnetic field \( 10^{14} \div 10^{15} \text{ G} \), called magnetars. These magnetars could be responsible for cosmological GRB, and may represent a plausible model for SGR. In the subsequent paper (Duncan & Thompson, 1995)
the connection between magnetars and SGR was developed in more details. The authors presented a model for SGRs, and the energetic 1979 March 5 burst, based on the existence of neutron stars with magnetic fields much stronger than those of ordinary pulsars.

Subsequent observations of $P$ and $\dot{P}$ in several SGR (McGill, 2014), seems to support this model. However, when the rotation energy losses are much less than observed X-ray luminosity, $B$ estimations using $\dot{P}$ are not justified, because magnetic stellar wind could be the main mechanism of angular momentum losses. The jump in $\dot{P}$ observed in the giant burst of PSR1900+14 (Fig.4) is plausibly explained by a corresponding increase of the magnetic stellar wind power, while the jump in the dipole magnetic field strength is hardly possible. The jumps in $P$, as well as in the pulse form (Figs.2,3) have not been seen in the radio pulsars. In the fall-back accretion model of SGR (Chatterjee et al., 2000; Alpar, 2001; Trümper et al., 2010; 2013) the estimations of the magnetic field using $P$ and $\dot{P}$ give the values characteristic for usual radiopulsars, when there is a presence of a large scale magnetic field in the fall back accretion disk (Bisnovatyi-Kogan & Ikhsanov, 2014).

When the energy density of the magnetic field is much larger than that of matter, as expected in the surface layers of the magnetar, the instability should be suppressed by magnetic forces. The observations of radio pulsars, showing no traces of bursts, with magnetar magnetic fields and slow rotation (Section), detection of SGR with a small rotational period and low magnetic field, estimated from $P$ and $\dot{P}$ values similar to radio pulsars (Section), gives a strong indication that inferred dipolar magnetic field strength and period cannot alone be responsible for the unusual high-energy properties of SGR/AXP. Therefore, another characteristic parameter should be responsible for a violent behaviour of SGR/AXP. The unusually low mass of the neutron star was suggested by Bisnovatyi-Kogan (2012), Bisnovatyi-Kogan and Ikhsanov (2014) as a parameter, distinguishing SGR/AXP neutron stars from the majority of neutron stars in radio pulsars and close X-ray binaries.

7. Angular momentum losses by a magnetized stellar wind

A magnetic stellar wind carries away the angular momentum $J$ as (Weber & Davis, 1967)

$$J_{\text{wind}} = \frac{2}{3} M \dot{\Omega} r_A^2,$$  

(1)

here $r_A$ is Alfvén radius, where the energy density of the wind $E_w$ is equal to the magnetic energy density $E_B = B^2/(8\pi)$. We consider the wind with a constant outflowing velocity $w$, which energy density is $E_w = 0.5\rho w^2$. In a stationary wind with a mass loss rate $\dot{M}$ the density is equal to

$$\rho = \frac{\dot{M}}{4\pi w r_A^2}. \quad (2)$$

For the dipole stellar field we have $B = \mu/r^3$, where $\mu = B_A r_A^3$ is the magnetic dipole moment of the star. At the Alfvén radius we have

$$\rho_A = \frac{\dot{M}}{4\pi w r_A^2}, \quad E_{w_A} = \frac{\dot{M} w}{8\pi r_A^3}, \quad E_{BA} = \frac{\mu^2}{8\pi r_A^3}. \quad (3)$$

From the definition of the Alfvén radius $r_A$ we obtain its value as

$$E_{wA} = E_{BA}, \quad r_A^4 = \frac{\mu^2}{Mw}. \quad (4)$$

The angular momentum of the star $J = I \dot{\Omega}$, and when the wind losses (1) are the most important, we obtain the value of stellar magnetic field as

$$B_{\text{wind}}^2 = \frac{9 I^2 \Omega^2 w}{4 \Omega^2 M r_A^6}. \quad (5)$$

The angular momentum and energy losses by the dipole radiation which are main losses in ordinary radio pulsars are written as (Pacini, 1967; Goldreich & Julian, 1969)

$$L = B_0^2 \Omega r_A^6, \quad \dot{E} = I \Omega \dot{\Omega} = L, \quad J_{\text{PRS}} = \frac{L}{\dot{\Omega}}. \quad (6)$$

We obtain from (6) the magnetic field if the dipole radiation losses are the most important

$$B_{\text{PSR}}^2 = \frac{3 I c^2 \dot{\Omega}}{20 \Omega r_A^6}. \quad (7)$$

The ratio of these two values is written as

$$\frac{B_{\text{PSR}}^2}{B_{\text{wind}}^2} = \frac{2 c^3 M}{3 I \Omega w} = \frac{4 \dot{M} w^2/2}{3 I \Omega} \left( \frac{c}{w} \right)^3 = \frac{4 F_{\text{wind}}}{3 E_{\text{rot}}} \left( \frac{c}{w} \right)^3. \quad (8)$$

Here $F_{\text{wind}}$ is the the energy flux carried away by the wind, and $E_{\text{rot}}$ is rate of the loss of rotational energy. For estimation of the energy flux carried away by the wind could be used the average X and $\gamma$-ray luminosity of SGR/AXP $L_{\gamma}$, and the wind velocity is of the order of the free fall velocity of the neutron star. For low mass neutron star $M \leq 0.8 M_\odot$ we have $v_{ff} = \sqrt{\frac{2GM}{r}} \approx \frac{c}{3}$ at $M = 0.6 M_\odot, r_* = 15$km, and

$$\frac{B_{\text{PSR}}^2}{B_{\text{wind}}^2} = 36 \frac{L_{\gamma}}{E_{\text{rot}}}. \quad (9)$$

Using data from McGill (2014) and (9) we obtain for the magnetic fields of SGR 0526-66, SGR 1806-20,
SGR 1900+14 the values $10^{13}$, $1.7 \cdot 10^{14}$, $6 \cdot 10^{13}$ Gs respectively. While the mechanical loss of the energy could exceed $L_{\gamma \gamma}$, these values of the magnetic field are suppose to be the upper limit if the magnetic field of these SGR, see Bisnovatyi-Kogan (2001).

8. Model of nuclear explosion

It was shown by Bisnovatyi-Kogan and Chechetkin (1974), that in the neutron star crust full thermodynamic equilibrium is not reached, and a non-equilibrium layer is formed there during a neutron star cooling, see also Bisnovatyi-Kogan (2001).

![Figure 5: The formation of chemical composition at the stage of limiting equilibrium. The thick line $Q_n = 0$ defines the boundary of the region of existence of nuclei, the line $Q_{nb}$ separates region I, where photo-disintegration of neutrons is impossible from regions II and III. The dashed lines indicate a level of constant $\varepsilon_\beta = Q_p - Q_n$; $\varepsilon_{\beta 1} < \varepsilon_{\beta 2} < \ldots < \varepsilon_{\beta \text{max}}$. In region I we have $Q_n > Q_{nb}$; in region II we have $Q_n < Q_{nb}$, $\varepsilon_{fe} < \varepsilon_\beta$; and in region III we have $Q_n < Q_{nb}$, $\varepsilon_{fe} > \varepsilon_\beta$. The line with the attached shading indicates a region of fission and $\alpha$-decay. The shaded region $abcd$ determines the boundaries for the values of $(A, Z)$ with a limited equilibrium situation, at given values of $Q_{nb}(T)$ and $\varepsilon_{fe}(\rho)$, from Bisnovatyi-Kogan and Chechetkin (1974).](image)

The non-equilibrium layer is formed in the region of densities and pressure $p_2 < \rho < p_1$, $P_1 < P < P_2$, with

$$\rho_1 \simeq \mu_e 10^6 \left(\frac{8}{0.511}\right)^3 \simeq 3.8 \cdot 10^9 \mu_e \text{ g/cm}^3$$

$$\simeq 1.5 \cdot 10^{10} \text{ g/cm}^3$$

$$\rho_2 \simeq \mu_e 10^6 \left(\frac{33}{0.511}\right)^3 \simeq 2.7 \cdot 10^{14} \mu_e \text{ g/cm}^3$$

$$\simeq 10^{12} \text{ g/cm}^3$$

$P_1 = 7.1 \cdot 10^{27}$ in cgs units, $P_2 = 2.1 \cdot 10^{30}$ in cgs units.

The mass of the non-equilibrium layer is defined as (Bisnovatyi-Kogan & Chechetkin, 1974)

$$M_{nl} = \frac{4\pi R^4}{GM} (P_2 - P_1) \simeq 0.1(P_2 - P_1) \simeq 2 \cdot 10^{29} \text{ g}$$

$$\simeq 10^{-4} M_\odot,$$

and the energy stored in this non-equilibrium layer is estimated as

$$E_{nl} \simeq 4 \cdot 10^{17} (P_2 - P_1) \approx 10^{48} \text{ erg}$$

Here a neutron star of a large ($\sim 2 M_\odot$) was considered, where the nonequilibrium layer is relatively thin, and its mass, and the energy store are estimated in the approximation of a flat layer. The nuclei in the nonequilibrium layer are overabundant with neutrons, so the number of nucleons per one electron is taken as $\mu_e \simeq 4$, and the energy release in the nuclear reaction of fission is about $5 \cdot 10^{-3} c^2 \text{ erg/g}$. Soon after discovery of gamma ray bursts the model of nuclear explosion was suggested (Bisnovatyi-Kogan et al., 1975), in which the non-equilibrium layer matter is brought to lower densities during a starquake. At the beginning GRB have been considered as objects inside the Galaxy, and the outburst was connected with period jumps in the neutron star rotation similar to those observed in the Crab nebula pulsar. It was suggested that: "Ejection of matter from the neutron stars may be related to the observed jumps of periods of pulsars. From the observed gain of kinetic energy of the filaments of the Crab Nebula ($\sim 2 \cdot 10^{43} \text{ erg}$) the mass of the ejected material may be estimated as ($\sim 10^{21} \text{ g}$). This leads to energies of the $\gamma$-ray bursts of the order of $10^{38} - 10^{40} \text{ erg}$, which agrees fully with observations at the mean distance up to the sources $0.25 \text{ kpc}$. A more detailed model of the strong 5 March 1979 burst, now classified as SGR 0526-66 in LMC, was considered by Bisnovatyi-Kogan and Chechetkin (1981). It was identified with an explosion on the NS inside the galactic disk, at a distance $\sim 100 \text{ ps}$. The schematic picture of the nuclear explosion of the matter from the non-equilibrium layer is presented in Fig.6.

![Figure 6: The schematic picture of non-equilibrium layer in the neutron star: a) in a quiescent stage; b) after starquake and nuclear explosion, from Bisnovatyi-Kogan (1992).](image)
Cosmological origin of GRB, and identification of a group of non-stationary sources inside Galaxy as SGR/AXP lead to considerable revision of the older model, presented by Bisnovatyi-Kogan et al. (1975). It becomes clear that SGR represent a very rare and very special type of objects, which produce bursts much more powerful, than it was thought before from comparison with quakes in Crab nebula pulsar. Besides, the SGR are the only sources for which the nuclear explosions could be applied, because the energy release in the cosmological GRB highly exceed the energy store in the non-equilibrium layer.

It was suggested by Bisnovatyi-Kogan (2012, 2015), Bisnovatyi-Kogan and Ikhsanov (2014), that the property, making the SGR neutron star so different from much more numerous of them in radio pulsars, single and binary X ray sources, is connected with the value of their mass, but not the magnetic field strength, see Camilo (2000), McLaughlin (2003), and Section . Namely, it was suggested that the neutron stars in SGR/AXP have anomalously low mass, \((0.4 \div 0.8)M_\odot\), compared to the well measured masses in binary systems of two neutron stars, where neutron stars have masses \(\geq 1.23M_\odot\) (Ferdman et al., 2014). The violent behaviour of the low-mass NS may be connected with much thicker and more massive non-equilibrium layer, and accretion from the fall-back highly magnetized accretion disk could trigger the instability, leading to outbursts explosions (Bisnovatyi-Kogan & Ikhsanov, 2014). The NS radius is increasing with mass rather slowly, and in a flat approximation the mass of non-equilibrium layer is inversely proportional to the mass. In Sect. the calculated mass of the non-equilibrium layer \(M_{nl} \approx 10^{-4}M_\odot\) was belonged to the neutron star with the mass \(\sim 2M_\odot\) (see Bethe & Johnson, 1975; Malone et al., 1975). It follows from calculations of neutron star models that for \(M_{ns} = 0.45M_\odot\) the mass of the non-equilibrium layer is \(\sim 7\) times larger (Bisnovatyi-Kogan & Ikhsanov, 2014). The energy store reaches \(\sim 10^{49}\) erg, what is enough for \(\sim 1000\) giant bursts.

The observational evidences for existence of neutron stars with masses, less than the Chandrasekhar white dwarf mass limit have been obtained by Janssen et al. (2008). Observations of the binary pulsar system J1518-4904 indicated the masses of the components to be \(m_p = 0.72(+0.51,-0.58)M_\odot\), \(m_e = 2.00(+0.58,-0.51)M_\odot\) with a 95.4% probability. It was suggested by Bisnovatyi-Kogan and Ikhsanov (2014) that low mass neutron stars could be formed in the scenario of the off-center explosion (Branch & Nomoto, 1986), but more detailed numerical investigation is needed to prove it. X-ray radiation of SGR/AXP in quiescent states was explained as a fall back accretion from the disk with a large scale poloidal magnetic field, what could also be a trigger for development of instability, leading to the mixing in the neutron star envelope, and nuclear explosion of the matter from the non-equilibrium layer.

9. Conclusions

1. SGR are highly active, slowly rotating neutron stars.
2. Nonequilibrium layer (NL) is formed in the neutron star crust, during NS cooling, or during accretion onto it. It may be important for NS cooling, glitches, and explosions connected with SGR.
3. The mass and the energy store in NL increase rapidly with decreasing of NS mass.
4. The properties of pulsar with high magnetic fields prove that inferred dipolar magnetic field strength and period cannot alone be responsible for the unusual high-energy properties of SGR/AXP. The NL in low mass NS may be responsible for bursts and explosions in them.
5. The upper boundary of the magnetic fields in 3 most famous SGR, measured by the average \(L_x\), luminosity is about one order of magnitude lower than the values obtained using the pulsar-like energy losses of the rotational energy of the neutron star.
6. Magnetar model of SGR, in which the energy of the observed bursts is provided by magnetic field annihilation, seems to be not relevant. Observations of quiet radiopulsars with a ”magnetar” magnetic field, and of a low-field ”magnetar”, is the most important indication to that conclusion. A rapid growth of rotational periods, what is a favorite argument for a ”magnetar” origin, is naturally explained by action of the magnetic stellar wind. Besides, the high pressure of the magnetic field suppresses convection, which is needed in all annihilation models.

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